## C2 Exponentials and Logarithms

1 Find, to 3 significant figures, the value of
a $\log _{10} 60$
b $\log _{10} 6$
c $\log _{10} 253$
d $\log _{10} 0.4$

2 Solve each equation, giving your answers to 2 decimal places.
a $10^{x}=14$
b $2\left(10^{x}\right)-8=0$
c $10^{3 x}=49$
d $10^{x-4}=23$
e $10^{2 x+1}=130$
f $100^{x}-5=0$

3 Show that $\log _{a} b=\frac{\log _{c} b}{\log _{c} a}$, where $a, b$ and $c$ are positive constants.
4 Find, to 3 significant figures, the value of
a $\log _{2} 7$
b $\log _{20} 172$
c $\log _{5} 49$
d $\log _{9} 4$

5 Solve each equation, giving your answers to 3 significant figures.
a $3^{x}=12$
b $\quad 2^{x}=0.7$
c $8^{-y}=3$
d $4^{\frac{1}{2} x}-0.3=0$
e $5^{t+3}=24$
f $\quad 16-3^{4+x}=0$
g $7^{2 x+4}=12$
h $5\left(2^{3 x+1}\right)=62$
i $\quad 4^{2-3 x}=32.7$
j $\quad 5^{x}=6^{x-1}$
k $7^{y+2}=9^{y+1}$
l $4^{5-x}=11^{2 x-1}$
m $4^{\frac{1}{2} x+3}-5^{1-2 x}=0$
n $2^{3 y-2}=3^{2 y+5}$
o $7^{2 x+5}=7\left(11^{3 x-4}\right)$
p $3^{2 x}=3^{x-1} \times 2^{4+x}$

6 Solve the following equations, giving your answers to 2 decimal places where appropriate.
a $2^{2 x}+2^{x}-6=0$
b $3^{2 x}-5\left(3^{x}\right)+4=0$
c $5^{2 x}+12=8\left(5^{x}\right)$
d $2\left(4^{x}\right)+3\left(4^{-x}\right)=7$
e $\quad 2^{2 y+1}+7\left(2^{y}\right)-15=0$
f $3^{2 x+1}-17\left(3^{x}\right)+10=0$
g $25^{t}+5^{t+1}-24=0$
h $3^{2 x+1}+15=2\left(3^{x+2}\right)$
i $3\left(16^{x}\right)-4^{x+2}+5=0$

7 Sketch each pair of curves on the same diagram, showing the coordinates of any points of intersection with the coordinate axes.
a $y=2^{x}$
$y=5^{x}$
b $y=3^{x}$
$y=\left(\frac{1}{3}\right)^{x}$
c $y=4^{x}$
$y=4^{x}-1$
d $y=2^{x}$
$y=2^{x+3}$

8 A curve has the equation $y=2+a^{x}$ where $a$ is a constant and $a>1$.
a Sketch the curve, showing the coordinates of any points of intersection with the coordinate axes and the equations of any asymptotes.
Given also that the curve passes through the point $(3,29)$,
b find the value of $a$.


The diagram shows the curve with equation $y=2^{x}-5$ which intersects the coordinate axes at the points $A$ and $B$. Find the length $A B$ correct to 3 significant figures.

